Magnetoresistance tensor of $\text{La}_{0.8}\text{Sr}_{0.2}\text{MnO}_3$

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We measure the temperature dependence of the anisotropic magnetoresistance (AMR) and the planar Hall effect (PHE) in *c*-axis-oriented epitaxial thin films of $La_{0.8}Sr_{0.2}MnO_3$ for different current directions relative to the crystal axes, and show that both AMR and PHE depend strongly on current orientation. We determine a magnetoresistance tensor, extracted to fourth order, which reflects the crystal symmetry and provides a comprehensive description of the data. We extend the applicability of the extracted tensor by determining the biaxial magnetocrystalline anisotropy in our samples.

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I. INTRODUCTION

The interplay between spin polarized-current and magnetic moments gives rise to intriguing phenomena that have led to the emergence of the field of spintronics.¹ In most cases, the materials used to study these phenomena have been amorphous alloys of three-dimensional (3D) itinerant ferromagnets (e.g., permalloy), while much less is known about the behavior in more complicated crystalline systems. Manganites, which are magnetic perovskites, serve as a good example for such a system. As we will show, elucidating these phenomena in this material system provides tools for better theoretical understanding of spintronics phenomena and reveals opportunities for novel device applications.

The magnetotransport properties of manganites, which are known for their colossal magnetoresistance, λ have been extensively studied; nevertheless, despite numerous studies devoted to elucidating the role of the magnitude of the magnetization, relatively few reports have addressed the role of the *orientation* of the magnetization, which is known to affect both the longitudinal resistivity ρ_{long} [anisotropic magnetoresistance effect (AMR)] and transverse resistivity ρ_{trans} [planar Hall effect (PHE)].

For conductors that are amorphous magnetic films, the dependence of ρ_{long} and ρ_{trans} on the magnetic orientation is given by

 $\rho_{\text{long}} = \rho_{\perp} + (\rho_{\parallel} - \rho_{\perp}) \cos^2 \varphi$

and

$$
\rho_{\text{trans}} = (\rho_{\parallel} - \rho_{\perp}) \sin \varphi \cos \varphi, \qquad (2)
$$

 φ (1)

where φ is the angle between the current **J** and the magnetization **M** and ρ_{\parallel} and ρ_{\perp} are the resistivities parallel and perpendicular to M, respectively.^{3[–6](#page-3-4)} Equations (1) (1) (1) and (2) (2) (2) are not expected to apply to crystalline conductors, as they are independent of the crystal $axes$ ⁷ Nevertheless, they have been used to describe AMR and PHE in epitaxial films; $8-11$ qualitative and quantitative deviations were occasionally attributed to extrinsic effects.

Here, we quantitatively identify the crystalline contributions to AMR and PHE in epitaxial films of $La_{0.8}Sr_{0.2}MnO₃$ $(LSMO)$ and replace Eqs. (1) (1) (1) and (2) (2) (2) with equations that

provide a comprehensive description of the magnetotransport properties of LSMO. The equations are derived by expanding the resistivity tensor to fourth order and keeping terms consistent with the crystal symmetry.

AMR and PHE in manganites constitute an important aspect of their magnetotransport properties; hence, quantitative determination of these effects is essential for comprehensive understanding of the interplay between magnetism and transport in this class of materials. In addition, when the dependence of AMR and PHE on local magnetic configurations is known, the two effects can be used as a powerful tool for probing and tracking static and dynamic magnetic configurations in patterned structures. Moreover, as the magnitude of the AMR and PHE changes dramatically with current direction, the elucidation of the appropriate equations is crucial for designing novel devices with optimal properties that are based on these phenomena.

II. EXPERIMENT

We present here results measured on epitaxial thin films $(\sim 40 \text{ nm})$ of La_{0.8}Sr_{0.2}MnO₃ with a Curie temperature (T_C) of \sim 290 K grown on cubic single-crystal [001] SrTiO₃ substrates using off-axis magnetron sputtering. $\theta - 2\theta$ x-ray diffraction reveals *c*-axis-oriented growth (in the pseudocubic frame), with an out-of-plane lattice constant of ~ 0.3876 nm, and an in-plane lattice constant of ~ 0.3903 nm, consistent with coherently strained films. No impurity phases are detected. Rocking curves taken around the 001 and 002 reflections have a typical full width at half maximum of 0.05°. The film surfaces have been characterized using atomic force microscopy, which shows a typical root-mean-square surface roughness of ~ 0.2 nm. The samples were patterned using photolithography to create seven patterns on the same substrate. Each pattern has its current path at a different angle θ relative to the [100] direction $(\theta = 0^\circ, 15^\circ, 30^\circ, 45^\circ,$ 60° , 75° , 90°), with electrical leads that allow for AMR and PHE measurements (see Fig. [1](#page-1-0)). ρ_{long} and ρ_{trans} data obtained by applying a magnetic field of $H=4$ T in the plane of the film and rotating the sample around the $[001]$ axis.

III. RESULTS AND DISCUSSION

Figure [2](#page-1-1) presents ρ_{long} and ρ_{trans} for all seven patterns at *T*= 5, 125, and 300 K. At *T*= 300 K both ρ_{long} and ρ_{trans} seem

FIG. 1. (Color online) ρ vs *T* with (solid circles) and without (empty circles) an applied magnetic field of $H=4$ T. Inset: Sketch of the relative orientations of the current density **J**, magnetization **M**, and the crystallographic axes. ρ_{long} is measured between *A* and *B*, ρ_{trans} is measured between *B* and *C*.

to behave according to Eqs. (1) (1) (1) and (2) (2) (2) . However, contrary to these equations, the amplitude of ρ_{long} differs from the amplitude of ρ_{trans} ; moreover, they both change with θ , the angle between J and $\lceil 100 \rceil$.

The discrepancies increase as the temperature decreases, and at $T = 125$ K the variations in the amplitudes for measurements taken for different θ increase. Furthermore, the location of the extremal points are dominated by α , the angle between **M** and [100]. At $T=5$ K, the deviations are even more evident as the AMR measurements are no longer described with a sinusoidal curve. All these observations clearly indicate the need for a higher-order tensor to adequately describe the magnetotransport behavior of LSMO.

The resistivity tensor in a magnetic conductor depends on the direction cosines, α_i , of the magnetization vector, and can be expressed as a series expansion of powers of the α_i ,^{[12](#page-3-8)} giving

$$
\rho_{ij}(\alpha) = \sum_{k,l,m,...=1} (a_{ij} + a_{kij}\alpha_k + a_{klij}\alpha_k\alpha_l + a_{klmij}\alpha_k\alpha_l\alpha_m
$$

+ $a_{klmnij}\alpha_k\alpha_l\alpha_m\alpha_n + \cdots),$ (3)

where $i, j = 1, 2, 3$ and the *a*'s are expansion coefficients. As usual $\rho_{ij}(\alpha) = \rho_{ij}^s(\alpha) + \rho_{ij}^a(\alpha)$, where ρ_{ij}^s and ρ_{ij}^a are symmetric and antisymmetric tensors, respectively. As both AMR and PHE are symmetric, we use only ρ_{ij}^s for their expression. As we are interested only in the in-plane properties, we use the tensor expansion for crystals with *m*3*m* cubic-crystal structure.¹³ The fourth-order symmetric resistivity tensor ρ^s for this class of materials in the xy plane (as M , J and the measurements are all in the plane of the film) is given by

$$
\rho^{s} = \begin{pmatrix} C' + C_1' \alpha_1^2 + C_2' \alpha_1^4 & C_4' \alpha_1 \alpha_2 \\ C_4' \alpha_1 \alpha_2 & C' + C_1' \alpha_2^2 + C_2' \alpha_2^4 \end{pmatrix}.
$$
 (4)

When **J** is along θ we obtain

$$
\rho_{\text{long}} = A \cos(2\alpha - 2\theta) + B \cos(2\alpha + 2\theta) + C \cos(4\alpha) + D \tag{5}
$$

and

$$
\rho_{\text{trans}} = A \sin(2\alpha - 2\theta) - B \sin(2\alpha + 2\theta) \tag{6}
$$

with:

$$
A = (C'_1 + C'_2 + C'_4)/4,
$$

\n
$$
B = (C'_1 + C'_2 - C'_4)/4,
$$

\n
$$
C = C'_2/8,
$$

\n
$$
D = C' + C'_1/2 + 3C'_2/8.
$$

Equations (5) (5) (5) and (6) (6) (6) , which take into account the crystal symmetry, have four independent parameters *A*, *B*, *C*, and *D*) with which we fit (as shown in Fig. [2](#page-1-1)) at any given temperature and magnetic field a set of 14 different curves (seven AMR curves and seven PHE curves).

Parameter *A* is a coefficient of a term describing a noncrystalline contribution since $(\alpha - \theta)$ is the angle between **M**

> FIG. 2. (Color online) Longitudinal resistivity ρ_{long} (left) and transverse resistivity ρ_{trans} (right) vs α , the angle between the magnetization and [100], for different angles θ (the angle between the current direction and [100]) at different temperatures with an applied magnetic field of 4 T). The solid lines are fits to Eqs. (5) (5) (5) and (6) (6) (6) .

and **J** irrespective of their orientation relative to the crystal axes. On the other hand, parameters *B* and *C* are coefficients of terms that depend on the orientation of **M** and/or **J** relative to the crystal axes.

We note that adding the terms with the coefficient B (in both Eq. (5) (5) (5) and (6) (6) (6)) to the "*A*" term changes only the amplitude and the phase of the signal compared to Eqs. (1) (1) (1) and (2) (2) (2) : Eq. (5) (5) (5) can be written (for $C=0$) as

$$
\rho_{\text{long}} = E \cos(2\alpha - \phi_{\text{long}}) + D,\tag{7}
$$

where $E^2 = A^2 + B^2 + 2AB \cos 4\theta$ and $\sin \phi_{\text{long}} = \frac{A-B}{E} \sin(2\theta);$ and Eq. (6) (6) (6) can be written as

$$
\rho_{\text{trans}} = F \sin(2\alpha - \phi_{\text{trans}}),\tag{8}
$$

where $F^2 = A^2 + B^2 - 2AB \cos 4\theta$ and $\sin \phi_{\text{trans}} = \frac{A+B}{F} \sin 2\theta$. The amplitude of $\rho_{\text{trans}}(\alpha)$, *F*, varies with θ between a maximal value of $|A+B|$ for $\theta = \pm 45^{\circ}$ and a minimal value of $\left| A - B \right|$ for $\theta = 0, \pm 90^{\circ}$. On the other hand, the amplitude of $\rho_{\text{long}}(\alpha)$, *E*, obtains its maximal value $\left|A+B\right|$ at $\theta=0, \pm 90^{\circ}$ and its minimal value $|A - B|$ at $\theta = \pm 45^{\circ}$. When the *C* term is added it does not affect ρ_{trans} ; however, ρ_{long} behaves qualitatively differently.

We thus observe that the current direction affects quite dramatically the amplitude of the effect. At 125 K, for instance, the PHE amplitude for current at 45° relative to $[100]$ is more than 20 times larger than the PHE for current parallel to [100]. This means that appropriate selection of the current direction that takes into consideration crystalline effects is important for designing devices that use the PHE for magnetic sensor or magnetic memory applications.¹⁴

Figure [3](#page-2-0) presents the temperature dependence of *B*/*A* and *C*/*A*. Close to T_c both *B* and *C* are negligible relative to *A*; therefore, AMR and PHE measurements appear to fit Eqs. ([1](#page-0-0)) and (2) (2) (2) . At intermediate temperatures where *C* is still much smaller than A (while B and A are of the same order), the signal remains sinusoidal, although its deviation from Eqs. (1) (1) (1) and (2) (2) (2) becomes quite evident. At low temperatures, C is on the order of *B*, and the AMR signal is no longer sinusoidal.

We have performed similar measurements using LSMO films with various doping levels as well as films of $La_{1-x}Ca_xMnO_3$. The results clearly indicate the failure of Eqs. (1) (1) (1) and (2) (2) (2) and the applicability of Eqs. (5) (5) (5) and (6) (6) (6) . These results will be addressed elsewhere. We also note that

FIG. 3. (Color online) The ratios of the coefficients from Eqs. ([5](#page-1-2)) and ([6](#page-1-3)) $(B/A$ and C/A) (left axis) and the coefficient K_1 from Eq. ([9](#page-2-1)) (right axis) as a function of temperature.

when **J** is along one of the crystal axes (i.e., $\theta = 0.90^{\circ}$) Eq. ([5](#page-1-2)) reduces to $\rho_{\text{long}} = a_0 + a_1 \cos^2 \alpha + a_2 \cos^4 \alpha$, a form used before to describe the crystal contributions in various mag-netic films including epitaxial films of Fe (Ref. [15](#page-3-11)) and $Fe₃O₄$.^{[16](#page-3-12)} Therefore, it appears that Eqs. ([5](#page-1-2)) and ([6](#page-1-3)) may be applicable to a wide range of materials.

Going back to $La_{0.8}Sr_{0.2}MnO₃$, we would like to address the case when the AMR and PHE measurements are performed with low applied magnetic fields, where **M** is no longer parallel to **H**, due to intrinsic magnetocrystalline anisotropy.

Our LSMO films exhibit biaxial magnetocrystalline anisotropy with easy axes along $\langle 110 \rangle$ directions, a manifestation of in-plane cubic symmetry. When a field **H** is applied, the total free energy consists of the magnetocrystalline anisotropy energy and the Zeeman energy

$$
E = \frac{K_1}{4}\cos^2 2\alpha - MH\cos(\alpha - \beta),\tag{9}
$$

where K_1 is the magnetocrystalline anisotropy energy and β is the angle between H and $[100]$. The first term is respon-

> FIG. 4. (Color online) Left: PHE signal as a function of β , the magnetic field direction relative to the $\begin{bmatrix} 100 \\ 100 \end{bmatrix}$ $(H= 500 \text{ Oe and } T$ $= 50$ K). The line is a fit to Eq. (6) (6) (6) with α extracted using Eq. ([9](#page-2-1)). Right: PHE as a function of magnetic field. The sample is prepared with M along $[100]$, and the field is applied along $[1\bar{1}0]$. The line is a fit using Eq. (9) (9) (9) .

sible for the biaxial magnetocrystalline anisotropy with easy axes along $\alpha = \pm 45^{\circ}$ and $\alpha = \pm 135^{\circ}$. We have determined the value of K_1 at various temperatures (see Fig. [3](#page-2-0)) by switching the magnetization between the two easy axes (see Fig. [4](#page-2-2)). The extracted value of K_1 allows us by using Eqs. (5) (5) (5) , (6) (6) (6) , and (9) (9) (9) to fit the AMR and PHE data obtained with relatively low applied fields (e.g., 500 Oe), where M does not follow H (see Fig. [4](#page-2-2)).

IV. CONCLUSION

In summary, we have expanded the magnetoresistance tensor to fourth order keeping terms consistent with the symmetry of epitaxial films of LSMO and derived equations that provide a comprehensive description of AMR and PHE in LSMO films in a wide range of temperatures. The results shed light on the interplay between magnetism and electrical transport in this class of materials and may serve as a basis for further study of the microscopic origin of magnetotransport properties of LSMO and other manganites. The results contribute to the ability to monitor magnetic configurations via magnetotransport properties, a feature of particular importance in studying nanostructures, and will facilitate the design of devices that use AMR and PHE.

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